

SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR
(AUTONOMOUS)

B.Tech.II Year II Semester Regular Supplementary Examinations July/August-2025
STATISTICAL METHODS FOR DATA SCIENCE
CSE(Artificial Intelligence & DataScience)

Time: 3 Hours**Max. Marks: 70****PART-A**(Answer all the Questions **10 x 2 = 20 Marks**)

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|---|---|--|-----|----|----|
| 1 | a | Write Some Properties of Random Variables. | CO1 | L1 | 2M |
| | b | Define Population and Sample with Examples. | CO1 | L1 | 2M |
| | c | Write any Two Properties of Maximum Likelihood Estimation. | CO2 | L1 | 2M |
| | d | Define Estimation, Estimate and Estimator. | CO2 | L1 | 2M |
| | e | Define Interval Estimation with an Example. | CO3 | L1 | 2M |
| | f | Find the Lower, Upper Confidence Limits and also Confidence Coefficient for $P[0 \leq \theta \leq 1.5] = 0.90$. | CO4 | L3 | 2M |
| | g | What is Type-II Error? | CO5 | L1 | 2M |
| | h | Define Alternative Hypothesis. | CO5 | L1 | 2M |
| | i | What is the Difference between F-test and t-tests? | CO6 | L1 | 2M |
| | j | Write the Formula for Chi-square Test for Goodness of Fit. | CO6 | L1 | 2M |

PART-B(Answer all Five Units **5 x 10 = 50 Marks**)**UNIT-I**

- 2 A Random Variable X has the following Probability Function

x	0	1	2	3	4	5	6	7
P(x)	0	K	2K	2K	3K	K^2	$2K^2$	$7K^2+K$

Determine (i) K (ii) Evaluate $P(x \geq 6)$ and $P(0 < x < 5)$ (iii) Find the Minimum Value of K such that $P(x \leq K) > 0.5$ (iv) Mean

OR

- 3 In a competition of 1000 cases, the mean of a certain test is 14 and standard deviation 2.5. Assuming the distribution to be normal, find
- (i). How many students score between 12 and 15
(ii). How many students score above 18
(iii). How many students score below 8.

UNIT-II

- 4 In a watch repair shop, the service time in minutes is 14, 17, 27, 18, 12, 8, 22, 13, 19 and 12. Give a maximum likelihood estimate of mean service time with the assumption that the service time follows an exponential distribution with parameter λ .

OR

- 5 A training data set of 9 different values for mid semester (say X) and end semester (say Y) values are given by

X	10	7	3	16	9	1	7	10	8
Y	42	39	32	50	44	55	43	37	43

Assuming a linear relationship Y on X, Estimate the parameters by the method of least squares.

UNIT-III

- 6 a Out of 300 households in a town 123 have T.V sets, find 95% confidence limits to the true value of proportion of households with T.V sets in the whole town. CO3 L3 5M
- b In a certain newspaper, it was given that 5% of Canadians are illiterate and that 7% of Americans are illiterate. In a sample of 1005 Canadians and 1015 Americans, what should be the difference be at 95% level of significance. CO3 L1 5M

OR

- 7 a A random sample of size $n=100$ is taken from a population with $\sigma = 5.1$. Given that the sample mean . Construct 95% confidence interval for population mean μ . CO4 L3 5M
- b Among 11 patients in a certain study, the Standard Deviation of the property of interest was 5.8. In another group of 4 patients the S.D was 3.4. Construct a 95% confidence interval for the ratio of the variances of these two populations. CO4 L5 5M

UNIT-IV

- 8 a Let p be the probability that a coin will fall head in a single toss in order to test $H_0: p = 0.5$ against $H_1: p = 0.75$.The coin is tossed 5 times and H_0 is rejected if more than 3 heads are obtained. Calculate the probability of type-I error and power of test. CO5 L3 5M
- b Obtain best critical region for testing null hypothesis $H_0: \lambda = \lambda_0$ against $H_1: \lambda = \lambda_1$ for an exponential distribution $f(x, \lambda) = \lambda e^{-\lambda x}$ 5M

OR

- 9 State and prove Neyman-Pearson Fundamental Lemma. CO5 L3 10M

UNIT-V

- 10 A pair of dice are thrown 360 times and the frequency of each sum is indicated below: CO6 L4 10M

Sum	2	3	4	5	6	7	8	9	10	11	12
Frequency	8	24	35	37	44	65	51	42	26	14	14

Would you say that the dice are fair on the basis of the chi-square test at 0.05 level of significant?

OR

- 11 Samples of two types of electrical light blubs were tested for length of life and following data were obtained. CO6 L2 10M

	Type I	Type II
Sample Size	8	7
Sample Mean	1234 hrs	1036 hrs
Sample Standard Deviation	36 hrs	40 hrs

Is the difference in the means sufficient to warrant that Type I is superior to Type II regarding length of life.

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